ALPEN-ADRIA UNIVERSITÄT KLAGENFURT

INVITATION TO THE DOCTORAL SEMINAR

On the performance of the Euler-Maruyama scheme for multidimensional SDEs with discontinuous drift coefficient

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Chaired by Michaela Hitz | Department of Statistics

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ABSTRACT

In recent years, a number of results have been proven in the literature for strong approximation of d-dimensional stochastic differential equations (SDEs) with a drift coefficient that may have discontinuities in space. In many of these results it is assumed that the drift coefficient is piecewise Lipschitz continuous, i.e. that there exists a hypersurface $\Theta \subseteq \mathbb{R}^d$ such that the drift coefficient is Lipschitz continuous with respect to the intrinsic metric on $\mathbb{R}^d \setminus \Theta$, while the diffusion coefficient is Lipschitz and non-degenerate close to Θ.

In particular, the performance of the Euler-Maruyama scheme was studied for such d-dimensional systems of SDEs. For $d = 1$ it was recently proven that the Euler-Maruyama scheme achieves an L_p-error rate of order at least $1/2$, just like in the case of Lipschitz continuous coefficients. For general $d \in \mathbb{N}$ only an L_2-error rate of order at least $1/4$ was known until recently. In this talk we show that for any $d \in \mathbb{N}$ an L_p-error rate of order at least $1/2-$ is achieved. We also

illustrate our results with numerical examples.

The talk is based on joint work with Thomas Müller-Gronbach (University of Passau) and Larisa Yaroslavtseva (University of Graz).

We hope to see you there!